April 22, 1958

FILE MEMO

SUBJECT: Floating Point Multiple Precision Routines

Programs are attached which show the effectiveness of Stretch in doing double and triple precision arithmetic. (This gives the equivalent of 28-29 or 43-44 decimal digits.)

As was expected, the double precision routines were extremely straightforward and easy to program since the double precision accumulator eliminates most coupling effects between high and low order portions which ordinarily must be programmed.

The triple precision programs were written to see what was required when the coupling effects had to be considered. Even in these cases the programs are fairly simple compared to other computers in which this type of routine has to be interpretively coded in fixed point and then converted back to floating point. The operation, Store With Borrow, was originally conceived as a requirement for multiple precision addition to afford coupling facility but it was found unnecessary with the present configuration and it is recommended that it be dropped.

Note that no attempt was made to guarantee the accuracy of the lowest order bits. To do this requires doing arithmetic of almost the next higher precision. For example, to guarantee the low order bit in single precision requires almost the work of double precision.

AN Swe

DWS/jcv

cc:

D. W. Sweeney Product Planning Coordinator Project 7000

7000 Product Planning Pr 7000 Engineering Planning Mr. E. H. Bloch Mr. L. G. Allen Mr. H. G. Jones Mr. G. T. Paul Mr. S. G. Campbell

Coelie

	ION	Dou 1: AD2	ьle Э, МИ	Pee LTIPL	cision .Y, and DIVI D	PA	GÉ.	· / ·		DATE-INITIALS: 7257
LOCATION	CL	OP	М	CI	ADDRESS	I	3	ADDRESS PX L B OF	x	REMARKS
ADD								1 1 1		These soutines assume
a+0	N	AD	5		4					one operand in The
dtl	W	AD	5		K					accumulator. The other
										is in storage (K,L) and
										The result is left in
MULTIPLY							<b></b>			the accumulator.
dto	N	LCMD	5		Aregister	_			_	
d+1	U	SLO	3		Aregister					
a+2	$\mathcal{U}$	MPYD	5		/K		ļ	1 1 1		
d+3	W_	MPYC	5		L					
at4	N	MPYC	S		<u> </u>					
ngang an										
		****								
DIVIDE										
d+0	N	DIND	5		<u>K</u>					
d+1	N	5	5		Mregister					
d+2	Ň	MPYD	N		Ľ					
d+3	N	AD	5		R register					
d+4	K	DIVD.	5		K					
1+5	N	AD	5		M register					
ndar m										
Maria di Santa di S		•								
										•
										•
in a										
									-	
						-11		1		

APPLICATION: ADD, MULTIPLY, And DIVIDE PAGE. 2

DATE-INITIALS:

4/22/58 DWS

LOCATION	CL	OP	M	CI	ADDRESS	-	T	ADDRESS	REMARKS
ADD			<u>†</u>	1	·	·			These particula required
ato	V	LD	5		G				March in the
1	N	AD	S		L	1	<b></b>		 (E (a) and (KL) with
2	N	AD	5		F				Regardet in stand RST
3	W	AD	S		K	-			me marines an school of
4	V	5	5		R				
5	V	310	S		S				
				1					
		•						1 1 1	
MULTIPLY				Ι					
ato	$\mathcal{U}$	L	5		G	_			
1	U	MPYD	5		K				
ک	U	LCMD	5		F		·		
3	N	MPYC	S		6				
4	N	MPYC	5		K			· · ·	
5	V	5	S		R			1 1 1	
6	V	520	S		S			1 1	
DIVIDE	U	LD	5		F				-
	N	AD	5		G				
	N	DIYD	5		K			L	
	N	5	5		R				
	N	MPYD	N		L				
	N	AD	5		Register				
	N	DIVD	5		k				
	N	AD	5	1	R				
	V	5	S		R				
	U	SLO	5		S				4
								1 1 1	
-									
	]			and the second s					
		-	-						
					· ·	1			

APPLICATION: ADD

PAGE 3

DATE-INITIALS:

4/2-158

LOCATION	CL	OP	M	CI	ADDRESS	X	3	AJ PX	DDRI	SS OF	X.	REMARKS
2+0	U	4	PAB		F				1 1	1		The operands are
1	V	A	NAB		K					1		(F.C.H) and (K.L.M). The
2		BIN .	FL	M	a+4				L	1		recelt uplaces (F.G.H)
3	I	SWP	F		F			K	1	1	3	
4		BIN	NL	PSH	9+24					1		
5	$\mathcal{U}$	LD	5		F				<u> </u>	1		
6	N	AD.	5		K				<b></b>	1		
2		BIN	NL	Z	a+27				1	1		
8	U	5	5		F					1		
9	V	51.0	5		K				1	1.		
10	U	LD	5		M					1		
11	N	AD	5		H				1 1	1		
12	N	10	5		L					1	·	
13	N	AD	5		G					1		
14	N	A-D	5		K				<u> </u>	1		
15	V	SLO	5		H				1	1		
16	V	AD	N		H				1	1		
17	N	A.D	5		F				L. I.	1		
18	N	5	5		F				1.1	1		
19	·V	SLO	5		4				<u> </u>	1		
20	U	LD	5		4				1	1		
21	U	AD	5.		H					1		
22	U	S	S		4				i I.	1		
23	U	520	5		H end of	En	m	tin	1 1	1		
24	U	LD	5		K					1		
25	U	SLO	S	•	K				1	1		
26		B		a a station	dtll				1	<u>†</u>		
27	V	SLO	5		F					1		
28		B			9+9				1 1			
									1 1	1		
							2		1	1		
										1		
	1				and the second			1 · · · ·		1		
	1								1 1	1		ť
			1	2					<u> </u>	1		
				14 1						1		

( APPLICÀT	ION	Trip MU	ble i	Prece (PL)	ision .	PA	GE!	4		DATE-INITIALS: 7/2-/58 The S
LOCATION	CL	OP	M	CI	ADDRESS	I	J	ADDRESS PX L B OF	x	REMARKS
d+0	11	L	5		F			· · · · · · · · · · · · · · · · · · ·		The operande are
1	11	ICMD	5		F					(F.G. H) and (K.L.M).
2	N	MPYD	5	· ·	K					The result replaces
2	11	5	5		F					(F,G,H)
4	U	SLO	31		Rregister					
5	$\overline{m}$	Z	.5		H		1	1 1 1		
6	17	MPYD	5		K			1 1 1		
	N	MPYC	5		M			1 1 1		
	N	MAYC	5		Z.		1	1 1 1		
G	11	ICMD	<u> </u>		6		1			
10	17	MAVE	5		Ĺ	-		1 1 1		
11	N	NAIC	5		K			1 1 1		
	N	4-7	5		Racington		1	1 1 1		
15	177	510	5		A					· · · · · · · · · · · · · · · · · · ·
14	1	AD	1/		H					
	11	4-D	5		F					
	11	5	5		F		1			
12	111	SLD	<		6					
18	11	12	5		6					
19	11	H-D	5		4					
20	15	5	3		G		T			
20	11	510	5	1	H					
	10			1						
	+		1	1						
	+	<u>†</u>					1			
	+		1	1		_				
		-	1			1				
	1			1			T			
	+			1						
	+	1		1		1		1 1 1		
	+		1							
	+		1	1 .						
	1	- 1847 - 1	1	1		1		1 1		
	-1	1	1	1			1.			
	1	1	1	1						
	+	1	1	1	1					

-

APPLICATION: DIVIDE

PAGE. 5

1

APPLICATION: DIVIDE								5		DATE-DITIALS: TYDIS	
LOCATION	CL	OP	M	CI	ADDRESS	I	3	ADDRESS PX 1L B OF	X	REMARKS	
9+0	U	LD	S		F					The operands are	
1	11	AD	S		4					(FG. H) and (KL, M).	
2	N	DIVD	5		K					The result replaces	
3	N	5	5		F					(F.G.H).	
4	U	MIYD	N		14		L		<u> </u>		
5	N	AD	5		Register			·····			
6	N	DIYD	5		K						
?	V	5	5		15						
8	U	MPYD	N	1	16		<u> </u>				
9	V	LCMD	N.	1	F		<b> </b>				
10	N	MMC	5	<b>_</b>	M		<b></b>	<u> </u>			
11	N	AD	5		K register	·	ļ	1 11			
12	N	DIND	5		KI		ļ	1 1			
13	N	AD	5		6						
14	V	510	5	<u> </u>	H+		<b> </b>				
15	V	AD	N	1	<u>H</u>			<u>                                 </u>	ļ		
16	N	AD	N		E			<u></u>			
17	N	5	5		F				<u> </u>		
18	10	540	5		9	_	ļ				
- 19	11	12	15		<u> </u>		ļ		<b> </b>		
20	U	AD	15	ļ	H				<b> </b>		
21	V	5	15		9						
22	V	540	S		_/#		<b>_</b>	I	ļ		
	<b>_</b>			<u> </u>				<u>                                      </u>			
	<b>_</b>		ļ				·	<u> </u>			
			.						ļ		
			ļ		a ata ata a a a a a a a a		· <u> </u>		<u> </u>		
	1	1	<b>_</b>	- <b> </b>		<u></u>	+				
	1	:	<b>_</b>	+			+				
	1		<b> </b>	· <b> </b> · · · · · · · · · · · · · · · · · · ·							
•		L						<u> </u>			
			<u> </u>	+		· · · · · · · · · · · · · · · · · · ·	<u>                                     </u>				
		ļ	1				+				
	1										
1	1	1 · · · · · ·	1	1	a 📔 a statut de la Caracteria				1		