

Multiple Precision Programs for Stretch

The objective of the design of the registers and operation was directed towards a simplification program set for single-precision floating point operations. Additional operational specifications and instructions were inserted to facilitate the programming of multiple precision operations.

The following three programs illustrate the ease with which double precision operations are effected by Stretch. They are nominal accuracy programs, i.e. there is no rounding and low-order bit effects are ignored.

Add: $(DE) + (JK)$

1. Load $A \leftarrow (K)$
2. η Add $A \leftarrow (E)$
3. η Add $AE \leftarrow (J)$
4. η Add $AE \leftarrow (D)$

Multiply: $(DE) \cdot (JK)$

1. Load ~~A~~ (K)
2. MPY and Set T_1 (D)
3. Store A (T_2)
4. Load ~~A~~ (E)
5. MPY and Set T_3 (J)
6. Add AB and Store T_2 (T_2)
7. Load ~~A~~ (T_1)
8. MPY (T_3)
9. Add AB (T_2)

Divide: $(DE) \div (JK)$

1. Load A (D)
2. Load B (E)
3. DIV and Set T_0 (J)
4. Store A (T_2)
5. Store B (T_3)
6. -MPY (K)
7. Add AB T_3
8. DIV T_1
9. Add A T_2

The following program illustrates the ease of programming a triple precision addition in floating point with automatic sign control. Note that the only tests necessary are those to find the relative difference between exponents. The problem introduced is most multiple precision programs of interaction (e.g. borrow or carry) between data words which cannot all fit in the accumulators at once is handled by the operation, 'Borrow', which subtracts one from the magnitude of the Accumulator and stores the result in the specified register, then replaces ~~A~~ mantissa ~~by~~ $1/2$ and subtracts 47 from the Exponent.

Addition: $(DEF) + (JKL)$

Only two of the four possible paths are shown. The other two paths are the same if the factors (DEF) and (JKL) are interchanged. Further programming effort can considerably reduce the number of steps necessary in these other paths, but would be extra detail to this example.

(DEF) + (JKL)

1. Load A and set T_1 (D)
2. Compare exponents (J)
 $D \geq J$
3. Store S (T_2)
4. Load A and set T_3 (E)
5. Compare exponents (T_2)
 $J > E$
6. Load A (T_1)
7. n Add A and Store T_1 (T_2)
8. Load A (B)
9. m Add A (T_3)
10. m Add AB (K)
11. Store m B (T_3)
12. m Add A and Store T_1 (T_1)
13. Store m B (T_2)
14. Load A (F)
15. n Add A (L)
16. m Add AB (T_3)
17. Store m B (T_5)
18. m Add A (T_2)
19. Store m B (T_4)
20. m Add A and Store T_1 (T_1)
21. Load A (13)
22. m Add A (T_4)
23. m Add AB (15)

$J > D$ and $K \geq D$. *loop is not shown.*

$E \geq J$

6. Load A (T_1)
7. Compare (T_1)
8. Remove and Store T_3 (T_4)
9. Load A (K)
10. Load B (L)
11. m Add AB (F)
12. m Add AB (T_3)
13. m Add AB (T_2)
14. Store m B (T_5)
15. m Add A (T_3)
16. m Add AB (T_4)
17. Transfer (14.)



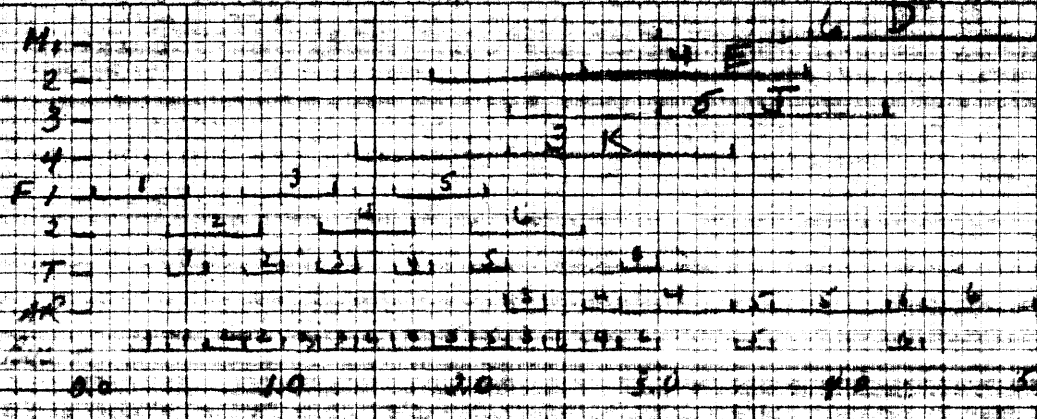
Multiplication (DEF) • (JKL)

Of the nine possible products only six are considered. These are

$$\begin{array}{r}
 D \cdot J \\
 + \quad D \cdot K \\
 + \quad E \cdot J \\
 + \quad D \cdot L \\
 + \quad E \cdot K \\
 + \quad F \cdot J
 \end{array}$$

- | | | | |
|------------------------------------|-------------------|------------------------------------|-------------------|
| 1. Load A, set T ₁ | (D) | 22. Load A | (T ₄) |
| 2. nMPYA, set T ₂ | (K) | 23. nMPYA | (F) |
| 3. Store A | (T ₅) | 24. n Add AB | (T ₃) |
| 4. Store B | (T ₆) | 25. n Add AB, store T ₂ | (T ₂) |
| 5. Load A, set T ₄ | (J) | 26. Store B | (T ₃) |
| 6. nMPYA, set T ₉ | (E) | 27. Load A | (T ₁) |
| 7. Store A | (T ₇) | 28. nMPYA | (L) |
| 8. Store B | (T ₂) | 29. n Add AC | (T ₂) |
| 9. Load A | (T ₁) | 30. n Add AC | (T ₃) |
| 10. nMPYA | (T ₄) | 31. n Add AC | (T ₆) |
| 11. n Add AB | (T ₅) | 32. n Add AB | (T ₄) |
| 12. n Add AC, store T ₅ | (T ₇) | 33. Store B | (T ₃) |
| 13. Store B | (T ₇) | 34. n Add A | (T ₇) |
| 14. n Sub S from AB | (S) | 35. n Add AC | (T ₅) |
| 15. Load A | (B) | | |
| 16. n Add A | (T ₆) | | |
| 17. n Add AB, store T ₆ | (T ₈) | | |
| 18. Store B | (T ₈) | | |
| 19. Load A | (T ₂) | | |
| 20. nMPYA, store T ₂ | (T ₃) | | |
| 21. Store B | (T ₃) | | |

ADD: (DE)+(JK)

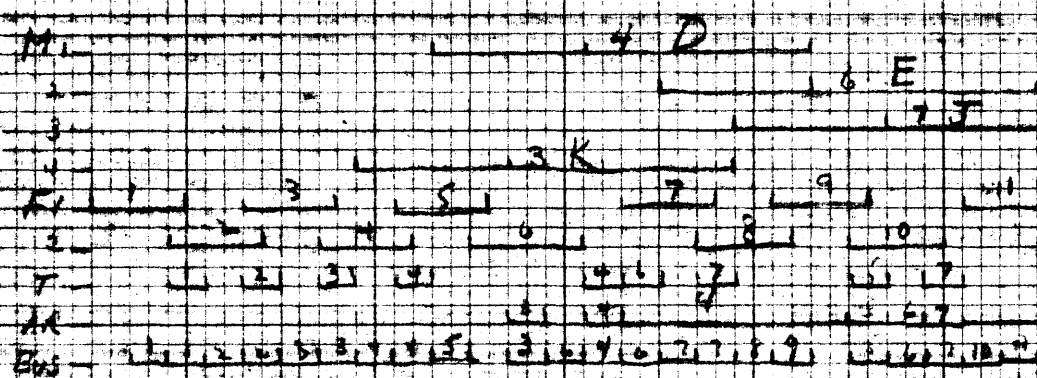


5.0µsec

$\frac{2.6}{5.0} = 52\%$

MPY: (DE)-(JK)

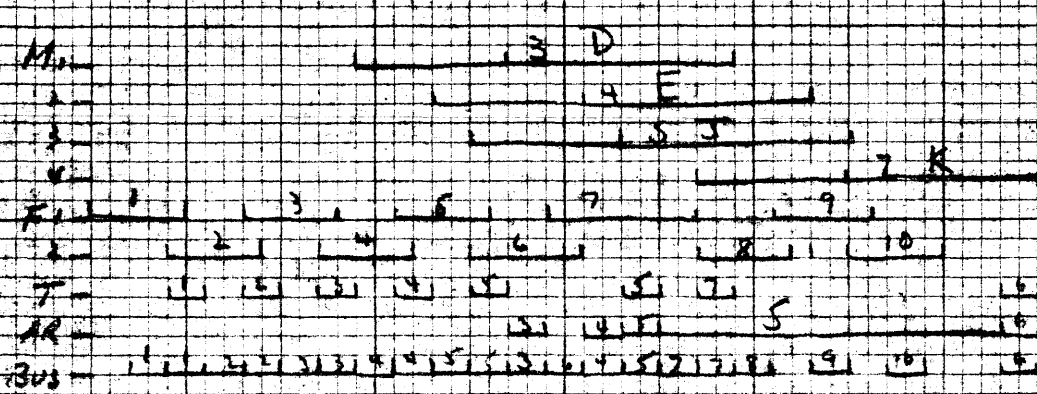
1. Setup 1
2. Setup 2
3. Load A (K)
4. MPY Set T₁ (D)
5. Setup A (T₂)
6. Load B (E)
7. MPY Set T₂ (J)
8. MPY Set T₂ (T₂)
9. Load B (T₁)
10. MPY (T₂)
11. MPY (T₂)



9.1µ

$\frac{4.7}{9.1} = 51.7\%$

DIV: (DE)/(JK)



9.9µsec

$\frac{7.5}{9.9} = 75.8\%$

1. Setup 1
2. Setup 2
3. Load A (D)
4. Load B (E)
5. DIV and Set T₁ (J)
6. Setup A (T₂)
7. MPY (K)
8. MPY (T₂)
9. DIV (T₁)
10. MPY (T₂)

Double Precision